

Prime Factorization

Lesson 1-1

Name: _____

Date: _____

Class: _____

Key Vocabulary

Level 1 support

Picture first, then the word, then a plain-language meaning. Say each word out loud.

7 has only two factors: 1×7 . So 7 is prime.

Prime number

A number bigger than 1 that you can only divide by 1 and itself.

$12 = 1 \times 12, 2 \times 6, 3 \times 4$ – six factors, so 12 is composite

Composite number

A number bigger than 1 that you can divide by more than just 1 and itself.

$$36 = 2 \times 2 \times 3 \times 3 = 2^2 \times 3^2$$

Prime factorization

Writing a number as prime numbers multiplied together.

$$24 \rightarrow 4 \times 6 \rightarrow (2 \times 2) \times (2 \times 3) \rightarrow 2 \times 2 \times 2 \times 3$$

Factor tree

A picture that splits a number into its prime numbers, step by step.

$$2^3 \text{ means } 2 \times 2 \times 2 = 8$$

Exponent

A small number that tells how many times to multiply a number by itself.

Key Ideas & Notes

- The space station received 60 supply crates.
- Mission Control needs to break this quantity into its prime components so the sorting robots can distribute them into equally sized pods.
- Help the crew find the prime factorization of 60!
- Sort these numbers – which are prime and which are composite?

Think About It

- What number are we breaking down into factors?
- What's the difference between a factor and a prime factor?
- How many different ways can we start breaking 60 apart?

My Notes

Guided Examples

Example 1

Which of the following is a prime number?

Solution: 17 has exactly two factors: 1 and 17. $15 = 3 \times 5$, $21 = 3 \times 7$, and $9 = 3 \times 3$, so they are all composite.

Answer: A. 17

Example 2

What is the prime factorization of 30?

Solution: $30 = 2 \times 15 = 2 \times 3 \times 5$. All three factors (2, 3, 5) are prime, so $2 \times 3 \times 5$ is the prime factorization.

Answer: A. $2 \times 3 \times 5$

Example 3

What is the prime factorization of 18?

Solution: $18 = 2 \times 9 = 2 \times 3 \times 3$. Both 2 and 3 are prime, so $2 \times 3 \times 3$ is the prime factorization.

Answer: A. $2 \times 3 \times 3$

Write About the Math

The Writing Revolution

I can explain how I broke a number down using the words prime number, composite number, factor, and exponent.

1. Kernel Sentence subject + verb

Model: Prime factorization is writing a number as prime numbers multiplied together.
Factorización prima es escribir un número como números primos multiplicados.

Write a kernel sentence about prime factorization. Use a subject and a verb.

Escribe una oración base sobre factorización prima. Usa un sujeto y un verbo.

2. Sentence Expansion because · but · so

Kernel: Prime factorization matters in math
Factorización prima importa en matemáticas

Expand the kernel three ways. Add a reason, a contrast, and a result.

because
porque

Prime factorization matters in math because ____.
Factorización prima importa en matemáticas porque ____.

but
pero

Prime factorization matters in math, but ____.
Factorización prima importa en matemáticas, pero ____.

so
entonces

Prime factorization matters in math, so ____.
Factorización prima importa en matemáticas, entonces ____.

3. Sentence Types 4 ways to write a math idea

Statement
Afirmación

Tell one true fact about prime factorization.
Di un hecho verdadero sobre prime factorization.

Prime factorization ____.

Question
Pregunta

Ask a question about prime factorization.
Haz una pregunta sobre prime factorization.

How does ____ ?

¿Cómo ____ ?

Exclamation
Exclamación

Show excitement about prime factorization.
Muestra entusiasmo sobre prime factorization.

Wow, ____ !

¡Guau, ____ !

Command
Mandato

Tell a partner what to do with prime factorization.
Dile a un compañero qué hacer con prime factorization.

First, ____ .

Primero, ____ .

4. Explain Your Reasoning use a sentence starter

I broke ____ **into** ____ **because** ____.

Separé ____ *en* ____ *porque* ____.

A prime number is ____.

Un número primo es ____.

This helps in real life when ____.

Esto ayuda en la vida real cuando ____.

Try It

Solve on your own. Check the answer key when you are done.

1. Which of these numbers is composite?

- A. 27
- B. 23
- C. 29
- D. 31

Show your work:

2. Two students found different factor trees for 60. Student A started with 2×30 . Student B started with 6×10 . Which statement is true?

- A. Both get the same prime factorization: $2 \times 2 \times 3 \times 5$
- B. Only Student A gets the correct prime factorization
- C. Only Student B gets the correct prime factorization
- D. They will get different prime factorizations

Show your work:

Stretch Your Thinking

Level 2 enrichment

Challenge task — explain your reasoning in full sentences.

Choose any two-digit composite number. Show TWO different factor trees that both lead to the same prime factorization. Explain why every composite number has only one prime factorization.

Sentence starter: I chose the number _____. My first factor tree starts with _____ × _____, and my second starts with _____ × _____. Both give the same prime factorization: _____. This happens because _____.

Show your work:

Reflect — Exit Ticket

What is the prime factorization of 40?

- A. $2 \times 2 \times 2 \times 5$
- B. 4×10
- C. 5×8
- D. 2×20

Your answer:

Answer Key & Teacher Guide

1. **Try It 1:** A. $27 - 27 = 3 \times 9 = 3 \times 3 \times 3$, so it has more than two factors. 23, 29, and 31 are all prime.
2. **Try It 2:** A. Both get the same prime factorization: $2 \times 2 \times 3 \times 5$ — *The Fundamental Theorem of Arithmetic says every composite number has exactly one prime factorization. No matter how you start the factor tree, you always end with $2 \times 2 \times 3 \times 5$.*
3. **Exit Ticket:** A. $2 \times 2 \times 2 \times 5 - 40 = 2 \times 20 = 2 \times 2 \times 10 = 2 \times 2 \times 2 \times 5$. All factors (2, 2, 2, 5) are prime.

Writing (TWR) — what to look for

- **Kernel sentence:** A complete sentence needs a subject and a verb. Example: Prime factorization is writing a number as prime numbers multiplied together.
- **Expansion:** *because* gives a reason, *but* shows a contrast or exception, *so* shows a result. Answers vary; each must keep the kernel idea and add the correct kind of detail.
- **Sentence types:** Statement ends with a period, question with "?", exclamation with "!", and a command starts with an action verb (a "bossy" verb).